

## **6-7 Solving Radical Equations and Inequalities**

**Solve each equation.**

1.  $\sqrt{x-4} + 6 = 10$

**SOLUTION:**

$$\sqrt{x-4} + 6 = 10$$

$$\sqrt{x-4} = 4$$

$$(\sqrt{x-4})^2 = 4^2$$

$$x-4 = 16$$

$$x = 20$$

2.  $\sqrt{x+13} - 8 = -2$

**SOLUTION:**

$$\sqrt{x+13} - 8 = -2$$

$$\sqrt{x+13} = 6$$

$$(\sqrt{x+13})^2 = 6^2$$

$$x+13 = 36$$

$$x = 23$$

3.  $8 - \sqrt{x+12} = 3$

**SOLUTION:**

$$8 - \sqrt{x+12} = 3$$

$$\sqrt{x+12} = 5$$

$$(\sqrt{x+12})^2 = 5^2$$

$$x+12 = 25$$

$$x = 13$$

## **6-7 Solving Radical Equations and Inequalities**

4.  $\sqrt{x-8} + 5 = 7$

**SOLUTION:**

$$\sqrt{x-8} + 5 = 7$$

$$\sqrt{x-8} = 2$$

$$\left(\sqrt{x-8}\right)^2 = 2^2$$

$$x-8 = 4$$

$$x = 12$$

5.  $\sqrt[3]{x-2} = 3$

**SOLUTION:**

$$\sqrt[3]{x-2} = 3$$

$$\left(\sqrt[3]{x-2}\right)^3 = 3^3$$

$$x-2 = 27$$

$$x = 29$$

6.  $(x-5)^{\frac{1}{3}} - 4 = -2$

**SOLUTION:**

$$(x-5)^{\frac{1}{3}} - 4 = -2$$

$$(x-5)^{\frac{1}{3}} = 2$$

$$\left((x-5)^{\frac{1}{3}}\right)^3 = 2^3$$

$$x-5 = 8$$

$$x = 13$$

## **6-7 Solving Radical Equations and Inequalities**

7.  $(4y)^{\frac{1}{3}} + 3 = 5$

**SOLUTION:**

$$(4y)^{\frac{1}{3}} + 3 = 5$$

$$(4y)^{\frac{1}{3}} = 2$$

$$\left((4y)^{\frac{1}{3}}\right)^3 = 2^3$$

$$4y = 8$$

$$y = 2$$

8.  $\sqrt[3]{n+8} - 6 = -3$

**SOLUTION:**

$$\sqrt[3]{n+8} - 6 = -3$$

$$\sqrt[3]{n+8} = 3$$

$$\left(\sqrt[3]{n+8}\right)^3 = 3^3$$

$$n+8 = 27$$

$$n = 19$$

9.  $\sqrt{y} - 7 = 0$

**SOLUTION:**

$$\sqrt{y} - 7 = 0$$

$$\sqrt{y} = 7$$

$$\left(\sqrt{y}\right)^2 = 7^2$$

$$y = 49$$

## 6-7 Solving Radical Equations and Inequalities

10.  $2 + 4z^{\frac{1}{2}} = 0$

**SOLUTION:**

$$2 + 4z^{\frac{1}{2}} = 0$$

$$4z^{\frac{1}{2}} = -2$$

$$z^{\frac{1}{2}} = -\frac{1}{2}$$

$$\sqrt{z} = -\frac{1}{2}$$

$$z = \frac{1}{4}$$

Check:

$$2 + 4\left(\frac{1}{4}\right)^{\frac{1}{2}} \stackrel{?}{=} 0$$

$$2 + 4\left(\frac{1}{2}\right) \stackrel{?}{=} 0$$

$$2 + 2 \stackrel{?}{=} 0$$

$$4 \neq 0 \times$$

Therefore, the equation has no solution.

11.  $5 + \sqrt{4y - 5} = 12$

**SOLUTION:**

$$5 + \sqrt{4y - 5} = 12$$

$$\sqrt{4y - 5} = 7$$

$$\left(\sqrt{4y - 5}\right)^2 = 7^2$$

$$4y - 5 = 49$$

$$4y = 54$$

$$y = \frac{27}{2}$$

## **6-7 Solving Radical Equations and Inequalities**

12.  $\sqrt{2t-7} = \sqrt{t+2}$

**SOLUTION:**

$$\sqrt{2t-7} = \sqrt{t+2}$$

$$(\sqrt{2t-7})^2 = (\sqrt{t+2})^2$$

$$2t-7 = t+2$$

$$t = 9$$

## **6-7 Solving Radical Equations and Inequalities**

13. **CCSS REASONING** The time  $T$  in seconds that it takes a pendulum to make a complete swing back and forth is given by the formula  $T = 2\pi\sqrt{\frac{L}{g}}$ , where  $L$  is the length of the pendulum in feet and  $g$  is the acceleration due to gravity, 32 feet per second squared.

- a. In Tokyo, Japan, a huge pendulum in the Shinjuku building measures 73 feet 9.75 inches. How long does it take for the pendulum to make a complete swing?
- b. A clockmaker wants to build a pendulum that takes 20 seconds to swing back and forth. How long should the pendulum be?

**SOLUTION:**

- a. Convert 73 feet 9.75 inches to feet.

$$73 \text{ feet } 9.75 \text{ inches} = 73 + \frac{9.75}{12} = 73.8125 \text{ ft.}$$

Substitute 73.8125 and 32 for  $L$  and  $g$  then simplify.

$$\begin{aligned} T &= 2\pi\sqrt{\frac{73.8125}{32}} \\ &\approx 9.5 \end{aligned}$$

Therefore, the pendulum takes about 9.5 seconds to complete a swing.

- b. Substitute 20 for  $T$  and 32 for  $g$ .

$$\begin{aligned} 20 &= 2\pi\sqrt{\frac{L}{32}} \\ \sqrt{\frac{L}{32}} &= \frac{10}{\pi} \\ \left(\sqrt{\frac{L}{32}}\right)^2 &= \left(\frac{10}{\pi}\right)^2 \\ \frac{L}{32} &= \frac{100}{\pi^2} \\ L &= \frac{32 \times 100}{\pi^2} \\ &\approx 324 \end{aligned}$$

The pendulum should be about 324 ft long.

## **6-7 Solving Radical Equations and Inequalities**

14. **MULTIPLE CHOICE** Solve  $(2y + 6)^{\frac{1}{4}} - 2 = 0$ .

**A**  $y = 1$

**B**  $y = 5$

**C**  $y = 11$

**D**  $y = 15$

**SOLUTION:**

$$(2y + 6)^{\frac{1}{4}} - 2 = 0$$

$$(2y + 6)^{\frac{1}{4}} = 2$$

$$\left( (2y + 6)^{\frac{1}{4}} \right)^4 = 2^4$$

$$(2y + 6) = 16$$

$$2y = 10$$

$$y = 5$$

Option B is the correct answer.

## 6-7 Solving Radical Equations and Inequalities

**Solve each inequality.**

15.  $\sqrt{3x+4} - 5 \leq 4$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $3x+4 \geq 0$ .

$$3x+4 \geq 0$$

$$3x \geq -4$$

$$x \geq -\frac{4}{3}$$

Solve  $\sqrt{3x+4} - 5 \leq 4$ .

$$\sqrt{3x+4} - 5 \leq 4$$

$$\sqrt{3x+4} \leq 9$$

$$(\sqrt{3x+4})^2 \leq 9^2$$

$$3x+4 \leq 81$$

$$3x \leq 77$$

$$x \leq \frac{77}{3}$$

The solution region is  $-\frac{4}{3} \leq x \leq \frac{77}{3}$ .



## 6-7 Solving Radical Equations and Inequalities

16.  $\sqrt{b-7} + 6 \leq 12$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $b - 7 \geq 0$ .

$$b - 7 \geq 0$$

$$b \geq 7$$

Solve  $\sqrt{b-7} + 6 \leq 12$ .

$$\sqrt{b-7} + 6 \leq 12$$

$$\sqrt{b-7} \leq 6$$

$$(\sqrt{b-7})^2 \leq 6^2$$

$$b - 7 \leq 36$$

$$b \leq 43$$

The solution region is  $7 \leq b \leq 43$ .

17.  $2 + \sqrt{4y-4} \leq 6$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $4y - 4 \geq 0$ .

$$4y - 4 \geq 0$$

$$4y \geq 4$$

$$y \geq 1$$

Solve  $2 + \sqrt{4y-4} \leq 6$ .

$$2 + \sqrt{4y-4} \leq 6$$

$$\sqrt{4y-4} \leq 4$$

$$(\sqrt{4y-4})^2 \leq 4^2$$

$$4y - 4 \leq 16$$

$$4y \leq 20$$

$$y \leq 5$$

The solution region is  $1 \leq y \leq 5$ .

## **6-7 Solving Radical Equations and Inequalities**

18.  $\sqrt{3a+3} - 1 \leq 2$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $3a + 3 \geq 0$ .

$$3a + 3 \geq 0$$

$$3a \geq -3$$

$$a \geq -1$$

Solve  $\sqrt{3a+3} - 1 \leq 2$ .

$$\sqrt{3a+3} - 1 \leq 2$$

$$\sqrt{3a+3} \leq 3$$

$$(\sqrt{3a+3})^2 \leq 3^2$$

$$3a + 3 \leq 9$$

$$3a \leq 6$$

$$a \leq 2$$

The solution region is  $-1 \leq a \leq 2$ .

## **6-7 Solving Radical Equations and Inequalities**

19.  $1 + \sqrt{7x - 3} > 3$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $7x - 3 \geq 0$ .

$$7x - 3 \geq 0$$

$$7x \geq 3$$

$$x \geq \frac{3}{7}$$

Solve  $1 + \sqrt{7x - 3} > 3$ .

$$1 + \sqrt{7x - 3} > 3$$

$$\sqrt{7x - 3} > 2$$

$$(\sqrt{7x - 3})^2 > 2^2$$

$$7x - 3 > 4$$

$$7x > 7$$

$$x > 1$$

The solution region is  $x > 1$ .

## **6-7 Solving Radical Equations and Inequalities**

20.  $\sqrt{3x+6} + 2 \leq 5$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $3x+6 \geq 0$ .

$$3x+6 \geq 0$$

$$3x \geq -6$$

$$x \geq -2$$

Solve  $\sqrt{3x+6} + 2 \leq 5$ .

$$\sqrt{3x+6} + 2 \leq 5$$

$$\sqrt{3x+6} \leq 3$$

$$\left(\sqrt{3x+6}\right)^2 \leq 3^2$$

$$3x+6 \leq 9$$

$$3x \leq 3$$

$$x \leq 1$$

The solution region is  $-2 \leq x \leq 1$ .

## **6-7 Solving Radical Equations and Inequalities**

21.  $-2 + \sqrt{9 - 5x} \geq 6$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $9 - 5x \geq 0$ .

$$9 - 5x \geq 0$$

$$5x \leq 9$$

$$x \leq \frac{9}{5}$$

Solve  $-2 + \sqrt{9 - 5x} \geq 6$ .

$$-2 + \sqrt{9 - 5x} \geq 6$$

$$\sqrt{9 - 5x} \geq 8$$

$$(\sqrt{9 - 5x})^2 \geq 8^2$$

$$9 - 5x \geq 64$$

$$5x \leq -55$$

$$x \leq -11$$

The solution region is  $x \leq -11$ .

## **6-7 Solving Radical Equations and Inequalities**

22.  $6 - \sqrt{2y+1} < 3$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $2y+1 \geq 0$ .

$$2y+1 \geq 0$$

$$2y \geq -1$$

$$y \geq -\frac{1}{2}$$

Solve  $6 - \sqrt{2y+1} < 3$ .

$$6 - \sqrt{2y+1} < 3$$

$$\sqrt{2y+1} > 3$$

$$(\sqrt{2y+1})^2 > 3^2$$

$$2y+1 > 9$$

$$2y > 8$$

$$y > 4$$

The solution region is  $y > 4$ .

## 6-7 Solving Radical Equations and Inequalities

Solve each equation. Confirm by using a graphing calculator.

23.  $\sqrt{2x+5} - 4 = 3$

**SOLUTION:**

$$\sqrt{2x+5} - 4 = 3$$

$$\sqrt{2x+5} = 7$$

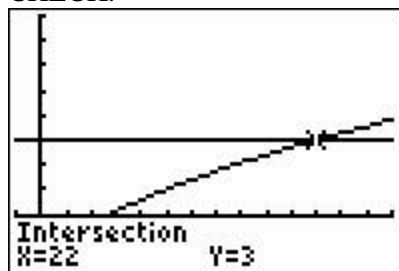
$$(\sqrt{2x+5})^2 = 7^2$$

$$2x + 5 = 49$$

$$2x = 44$$

$$x = 22$$

**CHECK:**



$[-2, 28]$  scl: 2 by  $[-2, 8]$  scl: 1

## 6-7 Solving Radical Equations and Inequalities

24.  $6 + \sqrt{3x+1} = 11$

**SOLUTION:**

$$6 + \sqrt{3x+1} = 11$$

$$\sqrt{3x+1} = 5$$

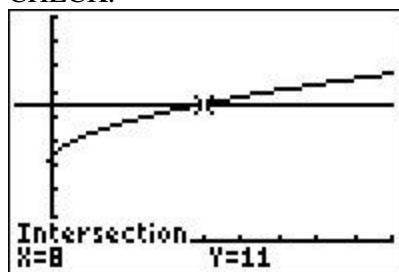
$$(\sqrt{3x+1})^2 = 5^2$$

$$3x+1 = 25$$

$$3x = 24$$

$$x = 8$$

**CHECK:**



$[-2, 18]$  scl: 2 by  $[-2, 18]$  scl:2



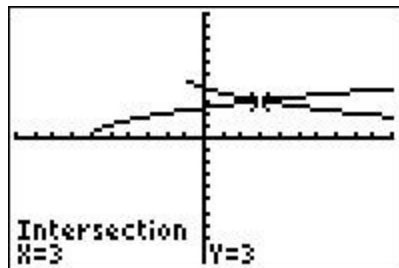
## 6-7 Solving Radical Equations and Inequalities

25.  $\sqrt{x+6} = 5 - \sqrt{x+1}$

**SOLUTION:**

$$\begin{aligned}\sqrt{x+6} &= 5 - \sqrt{x+1} \\ \sqrt{x+6} + \sqrt{x+1} &= 5 \\ (\sqrt{x+6} + \sqrt{x+1})^2 &= 5^2 \\ x+6 + x+1 + 2\sqrt{x^2+7x+6} &= 25 \\ 2\sqrt{x^2+7x+6} &= 18-2x \\ (2\sqrt{x^2+7x+6})^2 &= (18-2x)^2 \\ 4(x^2+7x+6) &= 324+4x^2-72x \\ 4x^2+28x+24 &= 324+4x^2-72x \\ 100x &= 300 \\ x &= 3\end{aligned}$$

**CHECK:**



[-10, 10] scl:1 by [-10, 10] scl:1

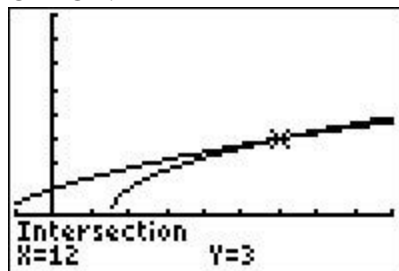
## 6-7 Solving Radical Equations and Inequalities

26.  $\sqrt{x-3} = \sqrt{x+4} - 1$

**SOLUTION:**

$$\begin{aligned}\sqrt{x-3} &= \sqrt{x+4} - 1 \\ \sqrt{x-3} - \sqrt{x+4} &= -1 \\ (\sqrt{x-3} - \sqrt{x+4})^2 &= 1^2 \\ x-3 + x+4 - 2\sqrt{x^2+x-12} &= 1 \\ 2\sqrt{x^2+x-12} &= 2x \\ (2\sqrt{x^2+x-12})^2 &= (2x)^2 \\ 4x^2 + 4x - 48 &= 4x^2 \\ 4x &= 48 \\ x &= 12\end{aligned}$$

**CHECK:**



$[-2, 18]$  scl: 2 by  $[-2, 8]$  scl: 1

## 6-7 Solving Radical Equations and Inequalities

27.  $\sqrt{x-15} = 3 - \sqrt{x}$

**SOLUTION:**

$$\sqrt{x-15} = 3 - \sqrt{x}$$

$$(\sqrt{x-15})^2 = (3 - \sqrt{x})^2$$

$$x - 15 = 9 + x - 6\sqrt{x}$$

$$-6\sqrt{x} = -24$$

$$\sqrt{x} = \frac{24}{6}$$

$$\sqrt{x} = 4$$

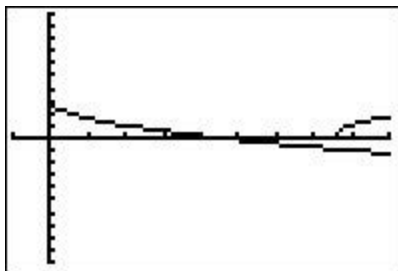
$$x = 16$$

Check:

$$\sqrt{16-15} \stackrel{?}{=} 3 - \sqrt{16}$$

$$\sqrt{1} \stackrel{?}{=} 3 - 4$$

$$1 \neq -1 \times$$



$[-2, 18]$  scl: 2 by  $[-10, 10]$  scl:1

There is no real solution for the equation.

## 6-7 Solving Radical Equations and Inequalities

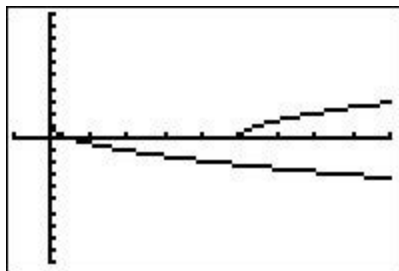
28.  $\sqrt{x-10} = 1 - \sqrt{x}$

**SOLUTION:**

$$\begin{aligned}\sqrt{x-10} &= 1 - \sqrt{x} \\ (\sqrt{x-10})^2 &= (1 - \sqrt{x})^2 \\ x - 10 &= 1 + x - 2\sqrt{x} \\ 2\sqrt{x} &= 11 \\ \sqrt{x} &= \frac{11}{2} \\ x &= \frac{121}{4}\end{aligned}$$

Check:

$$\begin{aligned}\sqrt{\frac{121}{4} - 10} &\stackrel{?}{=} 1 - \sqrt{\frac{121}{4}} \\ \sqrt{\frac{81}{4}} &\stackrel{?}{=} 1 - \frac{11}{2} \\ \frac{9}{2} &\neq -\frac{9}{2} \quad \times\end{aligned}$$



[-2, 18] scl: 2 by [-10, 10] scl:1

There is no real solution for the equation.

## 6-7 Solving Radical Equations and Inequalities

29.  $6 + \sqrt{4x + 8} = 9$

**SOLUTION:**

$$6 + \sqrt{4x + 8} = 9$$

$$\sqrt{4x + 8} = 3$$

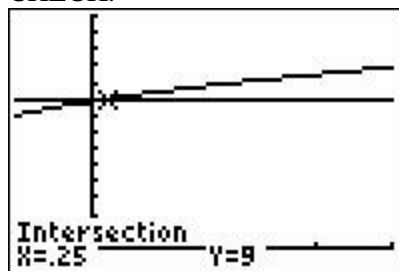
$$(\sqrt{4x + 8})^2 = 3^2$$

$$4x + 8 = 9$$

$$4x = 1$$

$$x = \frac{1}{4}$$

**CHECK:**



[-1, 4] scl: 1 by [-1, 14] scl: 1

30.  $2 + \sqrt{3y - 5} = 10$

**SOLUTION:**

$$2 + \sqrt{3y - 5} = 10$$

$$\sqrt{3y - 5} = 8$$

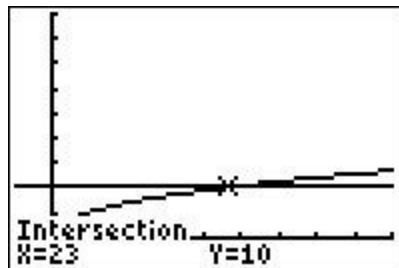
$$(\sqrt{3y - 5})^2 = 8^2$$

$$3y - 5 = 64$$

$$3y = 69$$

$$y = 23$$

**CHECK:**



[-5, 45] scl: 5 by [-5, 45] scl: 5

## 6-7 Solving Radical Equations and Inequalities

31.  $\sqrt{x-4} = \sqrt{2x-13}$

SOLUTION:

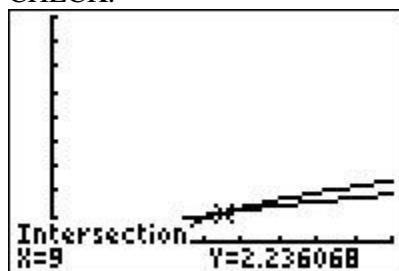
$$\sqrt{x-4} = \sqrt{2x-13}$$

$$(\sqrt{x-4})^2 = (\sqrt{2x-13})^2$$

$$x-4 = 2x-13$$

$$x = 9$$

CHECK:



[-2, 18] scl: 2 by [-2, 18] scl: 2

32.  $\sqrt{7a-2} = \sqrt{a+3}$

SOLUTION:

$$\sqrt{7a-2} = \sqrt{a+3}$$

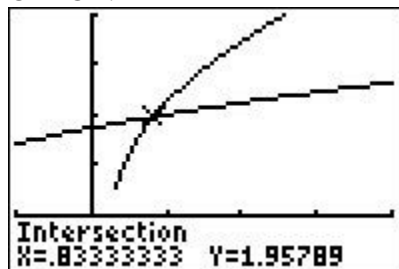
$$(\sqrt{7a-2})^2 = (\sqrt{a+3})^2$$

$$7a-2 = a+3$$

$$6a = 5$$

$$a = \frac{5}{6}$$

CHECK:



[-1, 4] scl: 1 by [-1, 4] scl: 1

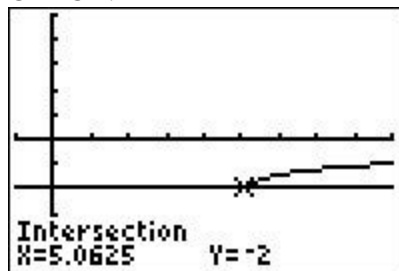
## 6-7 Solving Radical Equations and Inequalities

33.  $\sqrt{x-5} - \sqrt{x} = -2$

**SOLUTION:**

$$\begin{aligned}\sqrt{x-5} - \sqrt{x} &= -2 \\ (\sqrt{x-5} - \sqrt{x})^2 &= (-2)^2 \\ x-5 + x-2(\sqrt{x^2-5x}) &= 4 \\ 2\sqrt{x^2-5x} &= 2x-9 \\ (2\sqrt{x^2-5x})^2 &= (2x-9)^2 \\ 4x^2 - 20x &= 4x^2 + 81 - 36x \\ 16x &= 81 \\ x &= \frac{81}{16}\end{aligned}$$

**CHECK:**



$[-1, 9]$  scl: 1 by  $[-5, 5]$  scl: 1

## 6-7 Solving Radical Equations and Inequalities

34.  $\sqrt{b-6} + \sqrt{b} = 3$

**SOLUTION:**

$$\sqrt{b-6} + \sqrt{b} = 3$$

$$(\sqrt{b-6} + \sqrt{b})^2 = 3^2$$

$$b-6+b+2\sqrt{b^2-6b}=9$$

$$(2\sqrt{b^2-6b})^2 = (-2b+15)^2$$

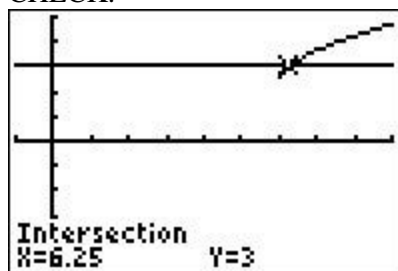
$$4b^2 - 24b = 4b^2 + 225 - 60b$$

$$36b = 225$$

$$b = \frac{225}{36}$$

$$b = \frac{25}{4}$$

**CHECK:**



$[-1, 9]$  scl: 1 by  $[-5, 5]$  scl: 1



## **6-7 Solving Radical Equations and Inequalities**

35. **CCSS SENSE-MAKING** Isabel accidentally dropped her keys from the top of a Ferris wheel. The formula

$t = \frac{1}{4}\sqrt{d-h}$  describes the time  $t$  in seconds at which the keys are  $h$  meters above the ground and Isabel is  $d$  meters above the ground. If Isabel was 65 meters high when she dropped the keys, how many meters above the ground will the keys be after 2 seconds?

**SOLUTION:**

Substitute 2 for  $t$  and 65  $d$ .

$$t = \frac{1}{4}\sqrt{d-h}$$

$$2 = \frac{1}{4}\sqrt{65-h}$$

$$\sqrt{65-h} = 8$$

$$(\sqrt{65-h})^2 = 8^2$$

$$65-h = 64$$

$$h = 1$$

The keys will be 1 meter above the ground after 2 seconds.

**Solve each equation.**

36.  $(5n-6)^{\frac{1}{3}} + 3 = 4$

**SOLUTION:**

$$(5n-6)^{\frac{1}{3}} + 3 = 4$$

$$(5n-6)^{\frac{1}{3}} = 1$$

$$\left((5n-6)^{\frac{1}{3}}\right)^3 = 1^3$$

$$5n-6 = 1$$

$$5n = 7$$

$$n = \frac{7}{5}$$

## **6-7 Solving Radical Equations and Inequalities**

37.  $(5p - 7)^{\frac{1}{3}} + 3 = 5$

**SOLUTION:**

$$(5p - 7)^{\frac{1}{3}} + 3 = 5$$

$$(5p - 7)^{\frac{1}{3}} = 2$$

$$\left( (5p - 7)^{\frac{1}{3}} \right)^3 = 2^3$$

$$5p - 7 = 8$$

$$5p = 15$$

$$p = 3$$

38.  $(6q + 1)^{\frac{1}{4}} + 2 = 5$

**SOLUTION:**

$$(6q + 1)^{\frac{1}{4}} + 2 = 5$$

$$(6q + 1)^{\frac{1}{4}} = 3$$

$$\left( (6q + 1)^{\frac{1}{4}} \right)^4 = 3^4$$

$$6q + 1 = 81$$

$$6q = 80$$

$$q = \frac{40}{3}$$

## 6-7 Solving Radical Equations and Inequalities

39.  $(3x + 7)^{\frac{1}{4}} - 3 = 1$

*SOLUTION:*

$$(3x + 7)^{\frac{1}{4}} - 3 = 1$$

$$(3x + 7)^{\frac{1}{4}} = 4$$

$$\left( (3x + 7)^{\frac{1}{4}} \right)^4 = 4^4$$

$$3x + 7 = 256$$

$$3x = 249$$

$$x = 83$$

40.  $(3y - 2)^{\frac{1}{5}} + 5 = 6$

*SOLUTION:*

$$(3y - 2)^{\frac{1}{5}} + 5 = 6$$

$$(3y - 2)^{\frac{1}{5}} = 1$$

$$\left( (3y - 2)^{\frac{1}{5}} \right)^5 = 1^5$$

$$3y - 2 = 1$$

$$3y = 3$$

$$y = 1$$

41.  $(4z - 1)^{\frac{1}{5}} - 1 = 2$

*SOLUTION:*

$$(4z - 1)^{\frac{1}{5}} - 1 = 2$$

$$(4z - 1)^{\frac{1}{5}} = 3$$

$$\left( (4z - 1)^{\frac{1}{5}} \right)^5 = 3^5$$

$$4z - 1 = 243$$

$$4z = 244$$

$$z = 61$$

## **6-7 Solving Radical Equations and Inequalities**

42.  $2(x-10)^{\frac{1}{3}} + 4 = 0$

**SOLUTION:**

$$2(x-10)^{\frac{1}{3}} + 4 = 0$$

$$2(x-10)^{\frac{1}{3}} = -4$$

$$\left(2(x-10)^{\frac{1}{3}}\right)^3 = (-4)^3$$

$$8(x-10) = -64$$

$$x-10 = -8$$

$$x = 2$$

43.  $3(x+5)^{\frac{1}{3}} - 6 = 0$

**SOLUTION:**

$$3(x+5)^{\frac{1}{3}} - 6 = 0$$

$$3(x+5)^{\frac{1}{3}} = 6$$

$$\left(3(x+5)^{\frac{1}{3}}\right)^3 = 6^3$$

$$27(x+5) = 216$$

$$x+5 = 8$$

$$x = 3$$

44.  $\sqrt[3]{5x+10} - 5 = 0$

**SOLUTION:**

$$\sqrt[3]{5x+10} - 5 = 0$$

$$\sqrt[3]{5x+10} = 5$$

$$\left(\sqrt[3]{5x+10}\right)^3 = 5^3$$

$$5x+10 = 125$$

$$5x = 115$$

$$x = 23$$

## **6-7 Solving Radical Equations and Inequalities**

45.  $\sqrt[3]{4n-8} - 4 = 0$

**SOLUTION:**

$$\sqrt[3]{4n-8} - 4 = 0$$

$$\sqrt[3]{4n-8} = 4$$

$$\left(\sqrt[3]{4n-8}\right)^3 = 4^3$$

$$4n - 8 = 64$$

$$4n = 72$$

$$n = 18$$

46.  $\frac{1}{7}(14a)^{\frac{1}{3}} = 1$

**SOLUTION:**

$$\frac{1}{7}(14a)^{\frac{1}{3}} = 1$$

$$(14a)^{\frac{1}{3}} = 7$$

$$\left((14a)^{\frac{1}{3}}\right)^3 = 7^3$$

$$14a = 343$$

$$a = 24.5$$

47.  $\frac{1}{4}(32b)^{\frac{1}{3}} = 1$

**SOLUTION:**

$$\frac{1}{4}(32b)^{\frac{1}{3}} = 1$$

$$(32b)^{\frac{1}{3}} = 4$$

$$\left((32b)^{\frac{1}{3}}\right)^3 = 4^3$$

$$32b = 64$$

$$b = 2$$

## **6-7 Solving Radical Equations and Inequalities**

48. **MULTIPLE CHOICE** Solve  $\sqrt[4]{y+2} + 9 = 14$ .

A 23

B 53

C 123

D 623

**SOLUTION:**

$$\sqrt[4]{y+2} + 9 = 14$$

$$\sqrt[4]{y+2} = 5$$

$$\left(\sqrt[4]{y+2}\right)^4 = 5^4$$

$$y+2 = 625$$

$$y = 623$$

Option D is the correct answer.

## **6-7 Solving Radical Equations and Inequalities**

49. **MULTIPLE CHOICE** Solve  $(2x-1)^{\frac{1}{4}} - 2 = 1$ .

**F** 41

**G** 28

**H** 13

**J** 1

**SOLUTION:**

$$(2x-1)^{\frac{1}{4}} - 2 = 1$$

$$(2x-1)^{\frac{1}{4}} = 3$$

$$\left( (2x-1)^{\frac{1}{4}} \right)^4 = 3^4$$

$$2x-1 = 81$$

$$2x = 82$$

$$x = 41$$

Option F is the correct answer.

## **6-7 Solving Radical Equations and Inequalities**

**Solve each inequality.**

50.  $1 + \sqrt{5x - 2} > 4$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $5x - 2 \geq 0$ .

$$5x - 2 \geq 0$$

$$5x \geq 2$$

$$x \geq \frac{2}{5}$$

Solve  $1 + \sqrt{5x - 2} > 4$ .

$$1 + \sqrt{5x - 2} > 4$$

$$\sqrt{5x - 2} > 3$$

$$(\sqrt{5x - 2})^2 > 3^2$$

$$5x - 2 > 9$$

$$5x > 11$$

$$x > \frac{11}{5}$$

The solution region is  $x > \frac{11}{5}$ .



## **6-7 Solving Radical Equations and Inequalities**

51.  $\sqrt{2x+14} - 6 \geq 4$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $2x + 14 \geq 0$ .

$$2x + 14 \geq 0$$

$$2x \geq -14$$

$$x \geq -7$$

Solve  $\sqrt{2x+14} - 6 \geq 4$ .

$$\sqrt{2x+14} - 6 \geq 4$$

$$\sqrt{2x+14} \geq 10$$

$$\left(\sqrt{2x+14}\right)^2 \geq 10^2$$

$$2x + 14 \geq 100$$

$$2x \geq 86$$

$$x \geq 43$$

The solution region is  $x \geq 43$ .

## **6-7 Solving Radical Equations and Inequalities**

52.  $10 - \sqrt{2x+7} \leq 3$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $2x+7 \geq 0$ .

$$2x+7 \geq 0$$

$$2x \geq -7$$

$$x \geq -\frac{7}{2}$$

Solve  $10 - \sqrt{2x+7} \leq 3$ .

$$10 - \sqrt{2x+7} \leq 3$$

$$-\sqrt{2x+7} \leq -7$$

$$\sqrt{2x+7} \geq 7$$

$$(\sqrt{2x+7})^2 \geq (7)^2$$

$$2x+7 \geq 49$$

$$2x \geq 42$$

$$x \geq 21$$

The solution region is  $x \geq 21$ .

53.  $6 + \sqrt{3y+4} < 6$

**SOLUTION:**

$$6 + \sqrt{3y+4} < 6$$

$$\sqrt{3y+4} < 0$$

Since the value of radical is nonnegative, the inequality has no real solution.

## **6-7 Solving Radical Equations and Inequalities**

54.  $\sqrt{2x+5} - \sqrt{9+x} > 0$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $2x+5 \geq 0$  and  $9+x \geq 0$ .

$$\begin{array}{ll} 2x+5 \geq 0 & \text{or } 9+x \geq 0 \\ 2x \geq -5 & \text{or } x \geq -9 \\ x \geq -\frac{5}{2} & \text{or } x \geq -9 \end{array}$$

Solve  $\sqrt{2x+5} - \sqrt{9+x} > 0$ .

$$\begin{array}{l} \sqrt{2x+5} - \sqrt{9+x} > 0 \\ \sqrt{2x+5} > \sqrt{9+x} \\ (\sqrt{2x+5})^2 > (\sqrt{9+x})^2 \\ 2x+5 > x+9 \\ x > 4 \end{array}$$

The solution region is  $x > 4$ .

## 6-7 Solving Radical Equations and Inequalities

55.  $\sqrt{d+3} + \sqrt{d+7} > 4$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $d+3 \geq 0$  and  $d+7 \geq 0$ .

$$\begin{array}{ll} d+3 \geq 0 & \text{or } d+7 \geq 0 \\ d \geq -3 & \text{or } d \geq -7 \end{array}$$

Solve  $\sqrt{d+3} + \sqrt{d+7} > 4$ .

$$\begin{aligned} \sqrt{d+3} + \sqrt{d+7} &> 4 \\ \left(\sqrt{d+3} + \sqrt{d+7}\right)^2 &> 4^2 \\ d+3+d+7+2\sqrt{d^2+10d+21} &> 16 \\ 2\sqrt{d^2+10d+21} &> 6-2d \\ \left(2\sqrt{d^2+10d+21}\right)^2 &> (6-2d)^2 \\ 4d^2+40d+84 &> 36+4d^2-24d \\ 64d &> -48 \\ d &> -\frac{3}{4} \end{aligned}$$

The solution region is  $d > -\frac{3}{4}$ .

## **6-7 Solving Radical Equations and Inequalities**

56.  $\sqrt{3x+9} - 2 < 7$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $3x+9 \geq 0$ .

$$3x+9 \geq 0$$

$$3x \geq -9$$

$$x \geq -3$$

Solve  $\sqrt{3x+9} - 2 < 7$ .

$$\sqrt{3x+9} - 2 < 7$$

$$\sqrt{3x+9} < 9$$

$$\left(\sqrt{3x+9}\right)^2 < 9^2$$

$$3x+9 < 81$$

$$3x < 72$$

$$x < 24$$

The solution region is  $-3 \leq x < 24$ .

## **6-7 Solving Radical Equations and Inequalities**

57.  $\sqrt{2y+5} + 3 \leq 6$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $2y + 5 \geq 0$ .

$$2y + 5 \geq 0$$

$$2y \geq -5$$

$$y \geq -\frac{5}{2}$$

Solve  $\sqrt{2y+5} + 3 \leq 6$ .

$$\sqrt{2y+5} + 3 \leq 6$$

$$\sqrt{2y+5} \leq 3$$

$$(\sqrt{2y+5})^2 \leq 3^2$$

$$2y + 5 \leq 9$$

$$2y \leq 4$$

$$y \leq 2$$

The solution region is  $-\frac{5}{2} \leq y \leq 2$ .

## **6-7 Solving Radical Equations and Inequalities**

58.  $-2 + \sqrt{8 - 4z} \geq 8$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $8 - 4z \geq 0$ .

$$8 - 4z \geq 0$$

$$4z \leq 8$$

$$z \leq 2$$

Solve  $-2 + \sqrt{8 - 4z} \geq 8$ .

$$-2 + \sqrt{8 - 4z} \geq 8$$

$$\sqrt{8 - 4z} \geq 10$$

$$(\sqrt{8 - 4z})^2 \geq 10^2$$

$$8 - 4z \geq 100$$

$$4z \leq -92$$

$$z \leq -23$$

The solution region is  $z \leq -23$ .

## **6-7 Solving Radical Equations and Inequalities**

59.  $-3 + \sqrt{6a+1} > 4$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $6a+1 \geq 0$ .

$$6a+1 \geq 0$$

$$6a \geq -1$$

$$a \geq -\frac{1}{6}$$

Solve  $-3 + \sqrt{6a+1} > 4$ .

$$-3 + \sqrt{6a+1} > 4$$

$$\sqrt{6a+1} > 7$$

$$\left(\sqrt{6a+1}\right)^2 > 7^2$$

$$6a+1 > 49$$

$$6a > 48$$

$$a > 8$$

The solution region is  $a > 8$ .



## 6-7 Solving Radical Equations and Inequalities

60.  $\sqrt{2} - \sqrt{b+6} \leq -\sqrt{b}$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $b+6 \geq 0$  and  $b \geq 0$ .

$$b+6 \geq 0$$

$$b \geq -6$$

Solve  $\sqrt{2} - \sqrt{b+6} \leq -\sqrt{b}$ .

$$\sqrt{2} - \sqrt{b+6} \leq -\sqrt{b}$$

$$\sqrt{b} - \sqrt{b+6} \leq -\sqrt{2}$$

$$(\sqrt{b} - \sqrt{b+6})^2 \leq (-\sqrt{2})^2$$

$$b + b + 6 - 2\sqrt{b^2 + 6b} \leq 2$$

$$2b - 2\sqrt{b^2 + 6b} \leq -4$$

$$b - \sqrt{b^2 + 6b} \leq -2$$

$$-\sqrt{b^2 + 6b} \leq -b - 2$$

$$(-\sqrt{b^2 + 6b})^2 \leq (-b - 2)^2$$

$$b^2 + 6b \leq b^2 + 4 + 4b$$

$$2b \leq 4$$

$$b \leq 2$$

The solution region is  $0 \leq b \leq 2$ .

## **6-7 Solving Radical Equations and Inequalities**

61.  $\sqrt{c+9} - \sqrt{c} > \sqrt{3}$

**SOLUTION:**

Since the radicand of a square root must be greater than or equal to zero, first solve  $c+9 \geq 0$  and  $c \geq 0$ .

$$c+9 \geq 0$$

$$c \geq -9$$

Solve  $\sqrt{c+9} - \sqrt{c} > \sqrt{3}$ .

$$\sqrt{c+9} - \sqrt{c} > \sqrt{3}$$

$$(\sqrt{c+9} - \sqrt{c})^2 > (\sqrt{3})^2$$

$$c+9+c-2\sqrt{c^2+9c} > 3$$

$$2\sqrt{c^2+9c} < 2c+6$$

$$(\sqrt{c^2+9c}) < (c+3)^2$$

$$c^2+9c < c^2+6c+9$$

$$3c < 9$$

$$c < 3$$

The solution region is  $0 \leq c < 3$ .

## 6-7 Solving Radical Equations and Inequalities

62. **PENDULUMS** The formula  $s = 2\pi\sqrt{\frac{\ell}{32}}$  represents the swing of a pendulum, where  $s$  is the time in seconds to swing back and forth, and  $\ell$  is the length of the pendulum in feet. Find the length of a pendulum that makes one swing in 1.5 seconds.

**SOLUTION:**

Substitute 1.5 for  $s$  and solve for  $\ell$ .

$$\begin{aligned}1.5 &= 2\pi\sqrt{\frac{\ell}{32}} \\ \sqrt{\frac{\ell}{32}} &= \frac{1.5}{2\pi} \\ \left(\sqrt{\frac{\ell}{32}}\right)^2 &= \left(\frac{1.5}{2\pi}\right)^2 \\ \frac{\ell}{32} &= \left(\frac{1.5}{2\pi}\right)^2 \\ \ell &= 32\left(\frac{1.5}{2\pi}\right)^2 \\ &\approx 1.82\end{aligned}$$

The length of the pendulum is about 1.82 ft.

63. **FISH** The relationship between the length and mass of certain fish can be approximated by the equation  $L = 0.46\sqrt[3]{M}$ , where  $L$  is the length in meters and  $M$  is the mass in kilograms. Solve this equation for  $M$ .

**SOLUTION:**

$$\begin{aligned}L &= 0.46\sqrt[3]{M} \\ \sqrt[3]{M} &= \frac{L}{0.46} \\ \left(\sqrt[3]{M}\right)^3 &= \left(\frac{L}{0.46}\right)^3 \\ M &= \left(\frac{L}{0.46}\right)^3\end{aligned}$$

## **6-7 Solving Radical Equations and Inequalities**

64. **HANG TIME** Refer to the information at the beginning of the lesson regarding hang time. Describe how the height of a jump is related to the amount of time in the air. Write a step-by-step explanation of how to determine the height of Jordan's 0.98-second jump.

**SOLUTION:**

If the height of a person's jump and the amount of time he or she is in the air are related by an equation involving radicals, then the hang time associated with a given height can be found by solving a radical equation.

65. **CONCERTS** The organizers of a concert are preparing for the arrival of 50,000 people in the open field where the concert will take place. Each person is allotted 5 square feet of space, so the organizers rope off a circular area of 250,000 square feet. Using the formula  $A = \pi r^2$ , where  $A$  represents the area of the circular region and  $r$  represents the radius of the region, find the radius of this region.

**SOLUTION:**

Substitute 250,000 for  $A$  and solve for  $r$ .

$$\begin{aligned} 250000 &= \pi r^2 \\ r^2 &= \frac{250000}{\pi} \\ \sqrt{r^2} &= \sqrt{\frac{250000}{\pi}} \\ r &= \frac{500}{\sqrt{\pi}} \\ &\approx 282 \end{aligned}$$

The radius of the region is about 282 ft.

## 6-7 Solving Radical Equations and Inequalities

66. **WEIGHTLIFTING** The formula  $M = 512 - 146,230B^{-\frac{8}{5}}$  can be used to estimate the maximum total mass that a weightlifter of mass  $B$  kilograms can lift using the snatch and the clean and jerk. According to the formula, how much does a person weigh who can lift at most 470 kilograms?

**SOLUTION:**

Substitute 470 for  $M$  and solve for  $B$ .

$$\begin{aligned}470 &= 512 - 146230B^{-\frac{8}{5}} \\146230B^{-\frac{8}{5}} &= 512 - 470 \\&= 42 \\B^{-\frac{8}{5}} &= \frac{42}{146230} \\B^{\frac{8}{5}} &= \frac{146230}{42} \\ \left(B^{\frac{8}{5}}\right)^{\frac{5}{8}} &= \left(\frac{146230}{42}\right)^{\frac{5}{8}} \\B &\approx 163.54\end{aligned}$$

The person weigh 163 kg can lift at most 470 kilograms.

67. **CCSS ARGUMENTS** Which equation does not have a solution?

$$\sqrt{x-1} + 3 = 4$$

$$\sqrt{x-2} + 7 = 10$$

$$\sqrt{x+1} + 3 = 4$$

$$\sqrt{x+2} - 7 = -10$$

**SOLUTION:**

$$\begin{aligned}\sqrt{x+2} - 7 &= -10 \\\sqrt{x+2} &= -3\end{aligned}$$

Since the value of the radical is negative, it does not have real solution.

## 6-7 Solving Radical Equations and Inequalities

68. **CHALLENGE** Lola is working to solve  $(x+5)^{\frac{1}{4}} = -4$ . She said that she could tell there was no real solution without even working the problem. Is Lola correct? Explain your reasoning.

**SOLUTION:**

Yes; since  $\sqrt[4]{x+5} \geq 0$ , the left side of the equation is nonnegative. Therefore, the left side of the equation cannot equal  $-4$ . Thus the equation has no solution.

69. **REASONING** Determine whether  $\frac{\sqrt{(x^2)^2}}{-x} = x$  is *sometimes*, *always*, or *never* true when  $x$  is a real number. Explain your reasoning.

**SOLUTION:**

$$\begin{aligned}\frac{\sqrt{(x^2)^2}}{-x} &= x \\ \frac{\sqrt{(x^2)^2}}{-x} &= x \\ \frac{x^2}{-x} &= x \\ x^2 &= (x)(-x) \\ x^2 &= -x^2\end{aligned}$$

But this is only true when  $x = 0$ . And in that case, we have division by zero in the original equation. So the equation is never true.

## **6-7 Solving Radical Equations and Inequalities**

70. **OPEN ENDED** Select a whole number. Now work backward to write two radical equations that have that whole number as solutions. Write one square root equation and one cube root equation. You may need to experiment until you find a whole number you can easily use.

**SOLUTION:**

Sample answer using 6:  $\sqrt{x-2} = 2, (x+21)^{\frac{1}{3}} = 3$

$$\sqrt{x-2} = 2$$

$$(\sqrt{x-2})^2 = 2^2$$

$$x-2 = 4$$

$$x = 6$$

$$(x+21)^{\frac{1}{3}} = 3$$

$$((x+21)^{\frac{1}{3}})^3 = 3^3$$

$$x+21 = 27$$

$$x = 6$$

71. **WRITING IN MATH** Explain the relationship between the index of the root of a variable in an equation and the power to which you raise each side of the equation to solve the equation.

**SOLUTION:**

They are the same number. For example,  $(\sqrt[3]{64})^3 = 64$ .

## 6-7 Solving Radical Equations and Inequalities

72. **OPEN ENDED** Write an equation that can be solved by raising each side of the equation to the given power.

a.  $\frac{3}{2}$  power

b.  $\frac{5}{4}$  power

c.  $\frac{7}{8}$  power

**SOLUTION:**

a. Sample answer:  $0 = 6x^{\frac{2}{3}} - 5$

b. Sample answer:  $0 = x^{\frac{4}{5}} - 9$

c. Sample answer:  $10x^{\frac{8}{7}} = -1$

73. **CHALLENGE** Solve  $7^{3x-1} = 49^{x+1}$  for  $x$ . (Hint:  $b^x = b^y$  if and only if  $x = y$ .)

**SOLUTION:**

$$7^{3x-1} = 49^{x+1}$$

$$7^{3x-1} = (7^2)^{x+1}$$

$$7^{3x-1} = 7^{2x+2}$$

Equate the powers and solve for  $x$ .

$$3x - 1 = 2x + 2$$

$$x = 3$$

**REASONING** Determine whether the following statements are *sometimes*, *always*, or *never* true for  $\frac{1}{x^n} = a$ . Explain your reasoning.

74. If  $n$  is odd, there will be extraneous solutions.

**SOLUTION:**

never;

Sample answer: The radicand can be negative.



## **6-7 Solving Radical Equations and Inequalities**

75. If  $n$  is even, there will be extraneous solutions.

**SOLUTION:**

sometimes;

Sample answer: when the radicand is negative, then there will be extraneous roots.

76. What is an equivalent form of  $\frac{4}{5+i}$ ?

**A**  $\frac{10-2i}{13}$

**B**  $\frac{5-i}{6}$

**C**  $\frac{6-i}{6}$

**D**  $\frac{6-i}{13}$

**SOLUTION:**

$$\begin{aligned}\frac{4}{5+i} &= \frac{4}{5+i} \cdot \frac{5-i}{5-i} \\ &= \frac{20-4i}{5^2-i^2} \\ &= \frac{20-4i}{25+1} \\ &= \frac{20-4i}{26} \\ &= \frac{10-2i}{13}\end{aligned}$$

Option A is the correct answer.

## **6-7 Solving Radical Equations and Inequalities**

77. Which set of points describes a function?

**F**  $\{(3, 0), (-2, 5), (2, -1), (2, 9)\}$

**G**  $\{(-3, 5), (-2, 3), (-1, 5), (0, 7)\}$

**H**  $\{(2, 5), (2, 4), (2, 3), (2, 2)\}$

**J**  $\{(3, 1), (-3, 2), (3, 3), (-3, 4)\}$

**SOLUTION:**

In option F and H, the element 2 has more than one image.

In option J, the elements 3 and  $-3$  have more than one image. In option G, every element has a unique image. So, it describes a function.

Therefore, option G is the correct answer.

78. **SHORT RESPONSE** The perimeter of an isosceles triangle is 56 inches. If one leg is 20 inches long, what is the measure of the base of the triangle?

**SOLUTION:**

Since the given triangle is an isosceles triangle, the measure of another leg should be 20 inches. Therefore, the measure of the base of the triangle is  $(56 - 20 - 20)$  or 16 in.

## **6-7 Solving Radical Equations and Inequalities**

79. **SAT/ACT** If  $\sqrt{x+5} + 1 = 4$ , what is the value of  $x$ ?

**A** 4

**B** 10

**C** 11

**D** 12

**E** 20

**SOLUTION:**

$$\begin{aligned}\sqrt{x+5} + 1 &= 4 \\ \sqrt{x+5} &= 3 \\ (\sqrt{x+5})^2 &= 3^2 \\ x+5 &= 9 \\ x &= 4\end{aligned}$$

Option A is the correct answer.

**Evaluate.**

80.  $27^{-\frac{2}{3}}$

**SOLUTION:**

$$\begin{aligned}27^{-\frac{2}{3}} &= \frac{1}{27^{\frac{2}{3}}} \\ &= \frac{1}{(3^3)^{\frac{2}{3}}} \\ &= \frac{1}{3^2} \\ &= \frac{1}{9}\end{aligned}$$

## 6-7 Solving Radical Equations and Inequalities

81.  $9^{\frac{1}{3}} \cdot 9^{\frac{5}{3}}$

**SOLUTION:**

$$\begin{aligned} 9^{\frac{1}{3}} \cdot 9^{\frac{5}{3}} &= 9^{\frac{1}{3} + \frac{5}{3}} \\ &= 9^2 \\ &= 81 \end{aligned}$$

82.  $\left(\frac{8}{27}\right)^{-\frac{2}{3}}$

**SOLUTION:**

$$\begin{aligned} \left(\frac{8}{27}\right)^{-\frac{2}{3}} &= \left(\frac{27}{8}\right)^{\frac{2}{3}} \\ &= \left(\frac{3^3}{2^3}\right)^{\frac{2}{3}} \\ &= \frac{3^2}{2^2} \\ &= \frac{9}{4} \end{aligned}$$

83. **GEOMETRY** The measures of the legs of a right triangle can be represented by the expressions  $4x^2y^2$  and  $8x^2y^2$ . Use the Pythagorean Theorem to find a simplified expression for the measure of the hypotenuse.

**SOLUTION:**

$$c = \sqrt{a^2 + b^2}$$

Substitute  $4x^2y^2$  and  $8x^2y^2$  for  $a$  and  $b$  and simplify.

$$\begin{aligned} c &= \sqrt{(4x^2y^2)^2 + (8x^2y^2)^2} \\ &= \sqrt{16x^4y^4 + 64x^4y^4} \\ &= \sqrt{16x^4y^4(1+4)} \\ &= 4x^2y^2\sqrt{5} \end{aligned}$$

Therefore, the measure of the hypotenuse is  $4x^2y^2\sqrt{5}$ .

## **6-7 Solving Radical Equations and Inequalities**

**Find the inverse of each function.**

84.  $y = 3x - 4$

**SOLUTION:**

$$y = 3x - 4$$

Interchange  $x$  and  $y$ , then solve for  $y$

$$x = 3y - 4$$

$$3y - 4 = x$$

$$3y = x + 4$$

$$y = \frac{x+4}{3}$$

85.  $y = -2x - 3$

**SOLUTION:**

$$y = -2x - 3$$

Interchange  $x$  and  $y$ , then solve for  $y$

$$x = -2y - 3$$

$$x + 2y = -3$$

$$2y = -x - 3$$

$$y = \frac{-x-3}{2}$$

86.  $y = x^2$

**SOLUTION:**

$$y = x^2$$

Interchange  $x$  and  $y$ , then solve for  $y$

$$y^2 = x$$

$$y = \pm \sqrt{x}$$

## 6-7 Solving Radical Equations and Inequalities

87.  $y = (2x + 3)^2$

**SOLUTION:**

$$y = (2x + 3)^2$$

Interchange  $x$  and  $y$  and solve for  $y$ .

$$(2y + 3)^2 = x$$

$$2y + 3 = \pm \sqrt{x}$$

$$2y = \pm \sqrt{x} - 3$$

$$y = \frac{\pm \sqrt{x} - 3}{2}$$

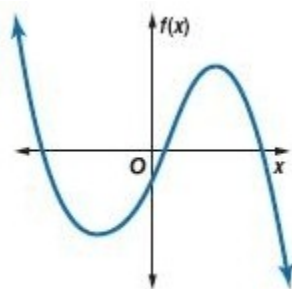
$$= \pm \frac{1}{2} \sqrt{x} - \frac{3}{2}$$

**For each graph,**

**a. describe the end behavior,**

**b. determine whether it represents an odd-degree or an even-degree polynomial function, and**

**c. state the number of real zeros.**



88.

**SOLUTION:**

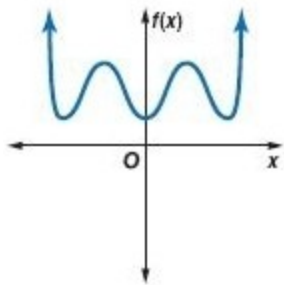
**a.** The function tends to  $+\infty$  as  $x$  tends to  $-\infty$ .

The function tends to  $-\infty$  as  $x$  tends to  $+\infty$ .

**b.** Since the end behaviors are in opposite directions, the graph represents an odd-degree polynomial.

**c.** Since the graph intersects the  $x$ -axis at three points, the number of real zeros is 3.

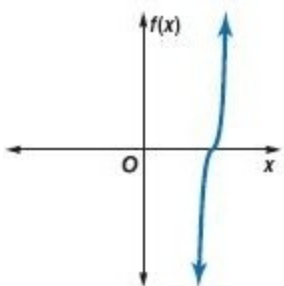
## 6-7 Solving Radical Equations and Inequalities



89.

**SOLUTION:**

- a. The function tends to  $+\infty$  as  $x$  tends to  $-\infty$  and  $+\infty$ .
- b. Since the end behaviors are in the same direction, the graph represents an even-degree polynomial.
- c. Since the graph does not intersect the  $x$ -axis, the number of real zeros is 0.



90.

**SOLUTION:**

- a. The function tends to  $+\infty$  as  $x$  tends to  $+\infty$ .  
The function tends to  $-\infty$  as  $x$  tends to  $-\infty$ .
- b. Since the end behaviors are in opposite directions, the graph represents an odd-degree polynomial.
- c. Since the graph intersects the  $x$ -axis at one point, the number of real zeros is 1.

## **6-7 Solving Radical Equations and Inequalities**

**Solve each equation. Write in simplest form.**

91.  $\frac{8}{5}x = \frac{4}{15}$

**SOLUTION:**

$$\begin{aligned}\frac{8}{5}x &= \frac{4}{15} \\ x &= \frac{4}{15} \cdot \frac{5}{8} \\ &= \frac{1}{6}\end{aligned}$$

92.  $\frac{27}{14}y = \frac{6}{7}$

**SOLUTION:**

$$\begin{aligned}\frac{27}{14}y &= \frac{6}{7} \\ y &= \frac{6}{7} \cdot \frac{14}{27} \\ &= \frac{4}{9}\end{aligned}$$

93.  $\frac{3}{10} = \frac{12}{25}a$

**SOLUTION:**

$$\begin{aligned}\frac{3}{10} &= \frac{12}{25}a \\ a &= \frac{3}{10} \cdot \frac{25}{12} \\ &= \frac{5}{8}\end{aligned}$$



## **6-7 Solving Radical Equations and Inequalities**

94.  $\frac{6}{7} = 9m$

**SOLUTION:**

$$\frac{6}{7} = 9m$$

$$m = \frac{6}{7} \cdot \frac{1}{9}$$
$$= \frac{2}{21}$$

95.  $\frac{9}{8}b = 18$

**SOLUTION:**

$$\frac{9}{8}b = 18$$

$$b = 18 \cdot \frac{8}{9}$$
$$= 16$$

96.  $\frac{6}{7}n = \frac{3}{4}$

**SOLUTION:**

$$\frac{6}{7}n = \frac{3}{4}$$

$$n = \frac{3}{4} \cdot \frac{7}{6}$$
$$= \frac{7}{8}$$

## **6-7 Solving Radical Equations and Inequalities**

$$97. \frac{1}{3}p = \frac{5}{6}$$

**SOLUTION:**

$$\frac{1}{3}p = \frac{5}{6}$$

$$p = \frac{5}{6} \cdot 3$$

$$= \frac{5}{2}$$

$$= 2\frac{1}{2}$$

$$98. \frac{2}{3}q = 7$$

**SOLUTION:**

$$\frac{2}{3}q = 7$$

$$q = 7 \cdot \frac{3}{2}$$

$$= \frac{21}{2}$$

$$= 10\frac{1}{2}$$